CORRECTION TO THE REVIEW "MATHEMATICAL THEORY OF CRACKS FORMED AS A RESULT OF BRITTLE FRACTURE" \ast

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In preparing a monograph on brittle fracture, I noticed that Eqs. (5.40) and (5.42) relating to the example of a crack in a strip subjected to equal and opposite concentrated forces a distance apart contained an error. The correct form of these equations is as follows:

$$\frac{P}{K \sqrt{L}} = \left(\frac{2}{\pi} \sin \frac{\pi l}{L} (1+\alpha^2)\right)^{1/2} \left[\operatorname{ch} \frac{\pi s}{2L} + \frac{(1+\nu)}{1+\alpha^2} \frac{\pi s}{4L} \operatorname{sh} \frac{\pi s}{2L} \operatorname{ctg}^2 \frac{\pi l}{2L} \right]^{-1}$$
(5.40)

$$\frac{P}{K \sqrt{L}} = 2 \left(\frac{1}{\pi} \operatorname{cotg} \frac{\pi l}{2L}\right)^{1/2}.$$
(5.42)

This error is linked with the incorrect computation of the sums of a series in [1]. The correct equation for the stress distribution in this problem takes the form

$$p(x) = \frac{P}{2\pi} \left\{ \left(\frac{\pi}{2L} \operatorname{sh} \frac{\pi s}{L} \right) \frac{1}{H} - (1+\nu) \frac{\pi^2}{4L^2} s\left(\operatorname{sh} \frac{\pi s}{L} \right) \frac{1}{H} + (1+\nu) \frac{\pi^2}{8L^2} s\left(\operatorname{sh}^2 \frac{\pi s}{L} \right) \frac{1}{H^2} \right\}, \quad H = \sin^2 \frac{\pi x}{2L} + \operatorname{sh}^2 \frac{\pi s}{2L}.$$

*PMTF, 1961, No. 4.

Moreover, in Eq. (5.10) a 2 was omitted from the numerator on the right side. It should also be noted that here, as in [1, 2], stress distributions corresponding to the plane state of stress were taken. The equations for plane strain are obtained by substituting $\nu/(1 - \nu)$ instead of ν .

REFERENCES

1. G. I. Barenblatt and G. P. Cherepanov, "Effect of the boundaries of a body on the development of brittle-fracture cracks," Izv. AN SSSR, OTN, Mekhanika i mashinostroenie, no. 3, 1960.

2. G. I. Barenblatt, "Equilibrium cracks associated with brittle fracture. Straight cracks in flat plates," PMM, vol. 23, no. 4, 1960.

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